

**STATE OF OHIO  
DEPARTMENT OF TRANSPORTATION**

**SUPPLEMENT 1040  
DETERMINATION OF STATISTICAL OUTLIERS**

**April 19, 2002**

**1040.01 Scope.** This supplement outlines the procedures for calculating statistical outliers in a sample set.

**1040.02 Definition.** An outlier is a sample that appears to deviate markedly from the other members of the sample set in which it occurs.

**1040.03 Calculation Procedure.**

1. Calculate the average ( $\bar{x}$ ) and standard deviation ( $\sigma$ ) of all the samples in the sample set.
2. Find the value of T from the attached table using the total number of samples (n) in the sample set.
3. Determine D (the total allowable deviation either side of  $\bar{x}$ ) by multiplying T by  $\sigma$ .
4. Establish values for MAX and MIN by adding and subtracting D to and from  $\bar{x}$ .
5. Any sample greater than MAX or less than MIN is an outlier.

**1040.04 Example.**

| Sample Set |    | Calculation          |                        |
|------------|----|----------------------|------------------------|
| 1A         | 41 | n = 10               | T (from table) = 2.290 |
| 1B         | 37 | $\bar{x} = 34.3$     |                        |
| 1C         | 41 | $\sigma = 5.8$       | $MAX = \bar{x} + D$    |
| 1D         | 37 |                      | $= 34.3 + 13.3$        |
| 2A         | 21 | $D = T \sigma$       | $= 47.6$               |
| 2B         | 30 | $= 2.290 \times 5.8$ | $MIN = \bar{x} - D$    |
| 2C         | 34 | $= 13.3$             | $= 34.3 - 13.3$        |
| 2D         | 33 |                      | $= 21.0$               |
| 3A         | 34 |                      |                        |
| 3B         | 35 |                      |                        |

Since Sample 2A(21) is equal to MIN (21.0) and Samples 1A and 1C (both 41) are less than MAX (47.6), there are no outliers in this sample set. If MIN had been calculated as 21.1, then Sample 2A would have been an outlier.

| n  | T     | n   | T     | n   | T     |
|----|-------|-----|-------|-----|-------|
|    |       | 51  | 3.136 | 101 | 3.386 |
|    |       | 52  | 3.143 | 102 | 3.390 |
| 3  | 1.155 | 53  | 3.151 | 103 | 3.393 |
| 4  | 1.481 | 54  | 3.158 | 104 | 3.397 |
| 5  | 1.715 | 55  | 3.166 | 105 | 3.400 |
| 6  | 1.887 | 56  | 3.172 | 106 | 3.403 |
| 7  | 2.020 | 57  | 3.180 | 107 | 3.406 |
| 8  | 2.126 | 58  | 3.186 | 108 | 3.409 |
| 9  | 2.215 | 59  | 3.193 | 109 | 3.412 |
| 10 | 2.290 | 60  | 3.199 | 110 | 3.415 |
| 11 | 2.355 | 61  | 3.205 | 111 | 3.418 |
| 12 | 2.412 | 62  | 3.212 | 112 | 3.422 |
| 13 | 2.462 | 63  | 3.218 | 113 | 3.424 |
| 14 | 2.507 | 64  | 3.224 | 114 | 3.427 |
| 15 | 2.549 | 65  | 3.230 | 115 | 3.430 |
| 16 | 2.585 | 66  | 3.235 | 116 | 3.433 |
| 17 | 2.620 | 67  | 3.241 | 117 | 3.435 |
| 18 | 2.651 | 68  | 3.246 | 118 | 3.438 |
| 19 | 2.681 | 69  | 3.252 | 119 | 3.441 |
| 20 | 2.709 | 70  | 3.257 | 120 | 3.444 |
| 21 | 2.733 | 71  | 3.262 | 121 | 3.447 |
| 22 | 2.758 | 72  | 3.267 | 122 | 3.450 |
| 23 | 2.781 | 73  | 3.272 | 123 | 3.452 |
| 24 | 2.802 | 74  | 3.278 | 124 | 3.455 |
| 25 | 2.822 | 75  | 3.282 | 125 | 3.457 |
| 26 | 2.841 | 76  | 3.287 | 126 | 3.460 |
| 27 | 2.859 | 77  | 3.291 | 127 | 3.462 |
| 28 | 2.876 | 78  | 3.297 | 128 | 3.465 |
| 29 | 2.893 | 79  | 3.301 | 129 | 3.467 |
| 30 | 2.908 | 80  | 3.305 | 130 | 3.470 |
| 31 | 2.924 | 81  | 3.309 | 131 | 3.473 |
| 32 | 2.938 | 82  | 3.315 | 132 | 3.475 |
| 33 | 2.952 | 83  | 3.319 | 133 | 3.478 |
| 34 | 2.965 | 84  | 3.323 | 134 | 3.480 |
| 35 | 2.979 | 85  | 3.327 | 135 | 3.482 |
| 36 | 2.991 | 86  | 3.331 | 136 | 3.484 |
| 37 | 3.003 | 87  | 3.335 | 137 | 3.487 |
| 38 | 3.014 | 88  | 3.339 | 138 | 3.489 |
| 39 | 3.025 | 89  | 3.343 | 139 | 3.491 |
| 40 | 3.036 | 90  | 3.347 | 140 | 3.493 |
| 41 | 3.046 | 91  | 3.350 | 141 | 3.497 |
| 42 | 3.057 | 92  | 3.355 | 142 | 3.499 |
| 43 | 3.067 | 93  | 3.358 | 143 | 3.501 |
| 44 | 3.075 | 94  | 3.362 | 144 | 3.503 |
| 45 | 3.085 | 95  | 3.365 | 145 | 3.505 |
| 46 | 3.094 | 96  | 3.369 | 146 | 3.507 |
| 47 | 3.103 | 97  | 3.372 | 147 | 3.509 |
| 48 | 3.111 | 98  | 3.377 |     |       |
| 49 | 3.120 | 99  | 3.380 |     |       |
| 50 | 3.128 | 100 | 3.383 |     |       |